

PATENT SPECIFICATION

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(54) APPARATUS FOR VARIABLY WEIGHTING RECEIVED ECHOES IN A MOVING TARGET INDICATOR RADAR

(71) We, WESTINGHOUSE ELECTRIC CORPORATION of 3 Gateway Center, Pittsburgh, Pennsylvania, United States of America, a Company organised and existing under the laws of the Commonwealth of Pennsylvania, United States of America, do hereby declare the invention, for which we pray that a patent may be granted to us, and the method by which it is to be performed, to be particularly described in and by the following statement:—

The present invention relates generally to moving target indicator (MTI) radars having variable interpulse period and more particularly relates to apparatus for variably weighting a sequence of individual echoes received from a target.

The employment of moving target indicators (MTI), to discriminate between radar echoes from moving targets and those from fixed or very slowly moving clutter, is well known. It involves the storage of a sequence of radar echoes and their vector summation in a canceller.

In the past, ultrasonic delay lines have been the most efficient and practical storage medium. Since each different interpulse period demanded a different delay line, both hardware cost and the difficulty of adjustment prevented the employment of more than two or three interpulse periods. Thus efforts to eliminate blind speeds in the velocity response were severely restricted and many regions of severe insensitivity, if not complete blindness, remained.

Storage tubes have been used in place of delay lines, and, more recently, digital storage devices have become competitive in price and superior in stability. These techniques of storage impose no restriction on interpulse period, and this freedom permits the radar designer to make a vast improvement in smoothing the velocity response in the speed range where desired targets are expected.

[Price 25p]

Unfortunately, there is a penalty associated with variable interpulse period (VIP). When the interpulse period is varied, the derivatives of interpulse period introduce degradation of the ideal clutter notch. One may suppress these degrading terms by making only very gradual changes in the interpulse period, but this is generally impractical because of the limited time in which the VIP sequence must be completed.

The chief object of the present invention is to provide apparatus for variably weighting a sequence of received echo pulses to provide the benefits of VIP without sacrificing the shape of the clutter notch for improving the clutter notch and to obtain a steep clutter notch by using four or more pulses without imposing impossible restrictions on how the interpulse period can be varied.

The invention resides in an MTI radar system comprising: means for generating pulse radar transmissions at variable time intervals, means for extracting one or both components of the echo vectors of said pulse radar transmissions, in-phase or in quadrature with a reference signal phase-locked to the pulse radar transmissions, means for sampling said component or components at regular intervals in range, means for converting each phase difference sample corresponding to a certain range cell into a digital word, means for storing at least a sequence of digital words corresponding to a same range cell, digital multiplying means for applying weighting coefficients to said sequence of stored digital words and to the most recent digital word corresponding to the same range cell as the sequence, said weighting coefficients being dependent upon the time intervals between all transmitted radar pulses corresponding to the digital words being weighted, means for summing said weighted sequence and most recent

word to obtain a digital representation of the sum, and means for converting said digital representation to an analog video display signal.

- 5 More specifically summing means are provided in a digital MTI radar system in the form of a multi-pulse canceller. The last received echo pulse and a sequence of pulses previously received are weighted by a
10 plurality of logic elements such as gates to improve the clutter notch. The weighting coefficients are not fixed values but are functions of the time separations between each of the series of echoes being processed.
15 Variation of interpulse period produces a coordinated variation in weighting coefficients to form a time-variable filter.

- A moving target indicator radar system is then provided permitting not only flexibility and choice of the interpulse period but also flexibility in the weighting of the pulses. The last received echo pulse and a sequence of previous pulses are provided with weighting factors in an arithmetic unit
20 of the radar receiver to provide the benefits of variable interpulse periods without sacrifice of the shape of the clutter notch reception. The weighting factors are selected to be binary in form to simplify the arithmetic
25 unit.

- Further objects and advantages of the present invention will be more readily apparent from the following detailed description taken in conjunction with the drawings,
30 in which:

Figure 1 is a graphical representation of the improved performance attainable when practicing the present invention;

- Fig. 2 is a vector diagram useful in understanding the operation of the present invention;

Fig. 3 is a schematic block diagram of an illustrative embodiment of the present invention; and

- 45 Fig. 4 is a schematic block diagram, in greater detail, of certain elements utilized in the illustrative embodiment of Fig. 3.

- In an MTI radar system utilizing a digital canceller, the radar receiver's phase detector output is sampled by an analog to digital converter in discrete range intervals. The analog to digital converter output is a digital word corresponding to the input amplitude.

- 55 The digital word for each range increment is stored in a separate location in a digital store device, such as a core memory. After one interpulse period, the stored digital word is read out and digitally subtracted from the new analog to digital converter output word.
60 Thus the core memory has introduced a delayed digital word for each range increment, analogous to the delay line in an analog canceller system. There is however
65 no restraint on the length of the interpulse

period as there is an analogue delay line system.

Moving targets will produce a doppler phase shift and be detected. Fixed targets will have no phase difference between successive returns and will cancel. The digital subtractor output is presented to an analog converter which provides the output MTI video.

The frequency response of such a simple two pulse canceller does not have as broad a clutter rejection notch in the vicinity of zero frequency, or as flat a pass band response as might be desired. By comparison of more than two successive received pulses and sinusoidally varying the interpulse period, a velocity response as indicated by the curve M in Fig. 1 is obtained.

The velocity response is shown with the velocity normalized so that $V=1$ represents the blind velocity associated with transmission at the average interpulse period. The ordinate is the enhancement of signal-to-noise ratio by the canceller in decibels. The velocity scale is logarithmic, so the ideal clutter notch associated with n pulses being compared in the canceller, assumes a slope of $(n-1)$; this is the response indicated for a fixed interpulse period system. When the interpulse period is varied, the first $(n-2)$ derivatives of interpulse period introduce degradation of the clutter notch. Fig. 1 shows by the curve M the effect on a four pulse canceller, but the degradation becomes more and more serious as the number of pulses in the canceller is increased.

One may suppress these degrading terms by making only very gradual changes in interpulse period, but this is generally impractical because of the limited time in which the VIP sequence must be completed. In order to insure the detection of a desired target, the VIP sequence must be completed within the time that the two-day beam pattern scans over the target. If the radar must detect not only the presence of the target but its location to a fraction of a beamwidth, several VIP sequences must be completed during the dwell time. Otherwise the echo will be strongest when the interpulse period is optimum, not when the antenna beam is centered on the target.

The velocity response curve M is obtained with about as gradual a VIP cycle as most radar dwell times can tolerate, the utilized pattern of deviation from average interpulse period is tabulated below:

-21.30	125
-20.63	
-17.29	
-11.27	
7.43	
14.78	130

	19.46
	21.47
	20.80
	17.46
5	11.44
	2.75
	- 7.26
	-14.61
	-19.29

10 This table is a parabolic approximation of a 16 pulse sinusoidal variation in the interpulse period. Actually, the radar would have benefitted from a wider deviation in
15 interpulse period than plus or minus 20%; the insensitivity at unit velocity could have been substantially reduced. However, wider deviation had to be sacrificed to prevent further notch degradation.

20 Typically, clutter in the radar beam must be suppressed by 40-60 db to make it small compared with the target of interest. The clutter has a velocity spectrum due to its motion (generally under one knot for trees,
25 even in high winds) and the motion of the tips of the antenna (generally several knots). Aircraft speeds vary from 60 knots upward, but the radial component of this speed is the only component detectable by the MTI, so
30 longer target range rates should be detectable. Ideally, targets below a critical range rate should be invisible, target above this range rate should be detectable with full sensitivity, regardless of their velocity. This
35 ideal MTI characteristic is more closely approximated than ever possible when practicing the present invention.

Figure 1 illustrates two ways in which variable weighting may be employed to improve the clutter notch. Curve N represents the ideal characteristic of slope 3, a significant improvement over the constant weighting case of curve M in the shape of the clutter notch. However, clutter suppression need not exceed a level determined by the radar cell size and the desired target of interest. At any selected level, the notch may be made 60% wider than the curve N by appropriate modification of weights.
50 Curve P shows a notch widened in this fashion: at the -51 db level; its width at this level is nearly double that of the constant weighted pulse response of curve M.

Four purposes of clarity, a four pulse canceller will be utilized as an example for deriving the necessary modification of weights for obtaining a desired velocity response in the critical clutter notch region. If the customary binomial weighting of the
60 four stored echoes is employed namely, 1,3,3,1, it will be shown that the output contains not only the desired cubic function of velocity, curve M of Fig. 1, but also degrading terms having slopes 2 and 1. A modification of the weighting factors will be de-

rived, which eliminates these degradations, and the example will illustrate the degree to which these optimum weightings may be approximated.

Let the magnitudes of weighting of pulses 70 A, B, C, and D be a , b , c , and d . The phase change between the echo pulses, which will be weighted and summed, is dependent upon target velocity (v) in radians per second and the interpulse period (T). Assuming a
75 reference which will be intermediate between the B and C pulse:

$$\theta_{BC} = \theta = v T_2$$

$$\theta_{AB} = \theta - \Delta\theta_1 = v T_1 = v T_2 - v(T_2 - T_1) \quad 80$$

$$\theta_{CD} = \theta + \Delta\theta_2 = v T_3 = v T_2 + v(T_3 - T_2)$$

The weighting factors applied to four 85 successive echoes of unit amplitude and their phase relationships are as illustrated in Fig. 2. Figure 2 illustrates the vector summation performed by the canceller on a
90 slow velocity target. All four echoes being compared are assumed to have identical amplitude (unity) so the amplitudes of the weighted echoes are a , b , c , and d . The four echoes have different phases because of the motion of the target. It is to be
95 noted that the phase difference between echoes B and C is θ . The zero or X axis is illustrated as a reference point between the echoes B and C. In other words the axis designated as X represents the phase of
100 a signal at the midpoint between the pulse echoes B and C.

It can be shown that for all conditions whether with modest or large steps of interpulse period that the coefficients of four
105 pulses in a sequence in the digital MTI radar namely for A, B, C and D the weighting factors a , b , c and d respectively are determined:

$$a \approx 1 + 3/2 (\Delta T_2/T_2) + 1/2 (\Delta T_2/T_2)^2 \quad 110$$

$$d \approx 1 - 3/2 (\Delta T_1/T_1) + 1/2 (\Delta T_1/T_2)^2 \quad 115$$

$$b \approx 4 - d - m - k$$

$$c \approx 4 - a - m - k \quad 120$$

where

$$m = 4 (\Delta T_1/T_2 - \Delta T_2/T_2) + [3 - 1/2 (\Delta T_1/T_2 - \Delta T_2/T_2)] (\Delta T_1/T_2) - (\Delta T_2/T_2)^2 \quad 125$$

a = coefficient of oldest echo.

b = coefficient of second oldest echo. 130

c = coefficient of third oldest echo.

d = coefficient of latest echo.

5 T_1 = interval between pulses weighted a and b .

T_2 = interval between pulses weighted b and c .

10 T_3 = interval between pulses weighted c and d .

$\Delta T_1 = T_2 - T_1$

15 $\Delta T_2 = T_3 - T_2$

k = constant which produces null in velocity response in the clutter notch region at the normalized velocity $V = \sqrt{k}/2\pi$, i.e. the abscisse of point R of curve P.

25 The choice of VIP sequence determines the response of the canceller to echoes from sources having radial velocities with the band of interest; 0.25 to 10, for example, may represent 25 to 1000 knot aircraft. Once the best VIP sequence is selected, the equations define the weighting coefficients which should be applied to the four echoes to provide the desired shape of response to echoes from low velocity sources; below 0.1, for example, may represent sources moving at less than 10 knots.

Assuming an extreme VIP characteristic of -25% , $0 + 25\%$, 0 deviation from average interpulse period the ideal values of the weighted factors can be shown to be:

Ideal Values	Pulses in Canceller			
	1234	2341	3412	4123
a'	1.434	1.135	.652	.832
45 b'	3.325	2.952	2.543	3.051
c'	2.543	2.952	3.325	3.051
d'	.652	1.135	1.434	.832

$K'/\sqrt{20} =$

50 $\sqrt{(a'^2 + b'^2 + c'^2 + d'^2)/20}$	1.004	.999	1.004	.999
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To convert these desired weighting factors to binary terms the weights must be rounded off to the low nearest least significant bit of $1/16$. The resultant values are:

	Pulses in canceller			
	1234	2341	3412	4123
60 a''	1.3750	1.1250	.6250	.8125
b''	3.3125	2.9375	2.5000	3.0000
c''	2.5000	2.9375	3.3125	3.0000
d''	.6250	1.1250	1.3750	.8125
65 $a'' - b'' + c'' - d''$	-.0625	.0000	+.0625	.0000
$K''/\sqrt{20}$.987	.993	.987	.983

The penultimate line of the above table shows that the sum $a'' - b'' + c'' - d''$ is not null in the first and third columns. To obtain $a'' - b'' + c'' - d''$ null, only the binary factors b'' and c'' are modified in each column whereas keeping the sensitivity of the canceller constant. The resultant values are:

	Pulses in canceller			
	1234	2341	3412	4123
a'''	1.3750	1.1250	.6250	.8125
b'''	3.1875	2.8750	2.4375	2.9375
c'''	2.4375	2.8750	3.1875	2.9375
d'''	.6250	1.1250	1.3750	.8125
75 $a''' - b''' + c''' - d'''$.0000	.0000	.0000	.0000
$K'''/\sqrt{20}$.96	.97	.96	.96

Once the weights have been successfully rounded off, implementation of the variable weighting factors in a digital MTI radar can be realized by reference to Figs. 3 and 4.

A stable oscillator 2 will provide a coherent reference frequency for the transmitter 4 as well as the clock frequency for a digital canceller 6. The incoming IF signal, after suitable filtering and amplification at 8 and 10 respectively, will be directly converted to bipolar video by phase comparison with the reference frequency. Both in-phase and quadrature channels 12 and 14 are provided to improve detectability and to allow phase information to be extracted after cancellation, if desired. The analog information at the output of the phase detectors is alternately fed to a sample and A to D converter 16 by a switching gate 18. The analog information containing one component of the echo vector is sampled at a 2.7 microsecond rate and converted into an eight bit digital word.

The digital canceller 6 is a four pulse digital canceller which implements an equation $aA - bB + cC - dD$, where again the capital letters represent successive echo components in a range bin. A magnetic core stack 19 of 512 range words \times 24 bits provides the necessary information storage.

The cancelled signals in both in-phase and quadrature channels are combined to provide an MTI video output.

A synchronizer 22 provides the necessary timing for the radar transmitter 4 as well as providing all internal timing for the canceller 6. All timing is derived from the 120 Megahertz reference oscillator 2. A VIP sequence control 24 provides a program to stagger the interpulse period in order to achieve the desired smooth velocity response. A time interval 26 inserts the desired variable interpulse period while a range counter 28 defines each range.

The pulse echo received from a target is amplified by the IF amplifier 10. The amplifier is chosen to have 20 Megahertz

bandwidth to provide well over 40 db gain. An attenuation control 30 is provided for exact adjustment of the gain. The amplifier 10 is preceded by a 200 Kiloherzt bandwidth crystal filter 8. The maximum input level required by the phase detectors 12 and 14 is +5 dbm (with respect to the watt) corresponding to a level of -43 dbm at the input of the IF amplifier when the phase signals are converted into 8-digit words which correspond to a sensitivity of -48 dbm. Since the noise input to the amplifier 10 is -80 dbm the gain of the amplifier will be adequate.

The phase detector is divided into two balanced sections 12 and 14 using Schottky barrier diodes as detectors. An input level is injected into each detector from the coho oscillator 2. This is mixed with the amplified received signals. The output from each is then filtered and sent to the A to D converter 16. A 90° adjustable phase shifter is increased in the out of phase or Q coho oscillator line to provide the desired quadrature phase relationship.

The bipolar video signal from the phase detectors 12 and 14 is sampled by the sample and hold circuit 16 and the amplitude is converted into a digital word. An in-phase (I) signal sample and a quadrature (Q) signal sample is taken through the switching gate 18 and converted every 5.4 microseconds. The output of the analog to digital converter 16 is selected to be seven bits of amplitude plus a sign bit. The I and Q channels are multiplexed into the A to D converter by the signal switch 18. (The linear dynamic range of the signal chain from the IF input to the A to D converter will be 50 db minimum).

The A to D converter 16 is a sequential converter using a voltage summing ladder network. The complete timing and control logic for the A to D converter and sample and hold circuits are self-contained and only two inputs are required to the converter 16; namely, the analog video and the sampling clock. When desirable, only the in phase (I) signal sample need be resolved in which instance the resolution time can be cut in half.

The four pulse canceller equation implemented in the canceller logic is: $F = aA - bB + cC - dD$. For one group of four pulses the weights may be: $a = 7/8$, $b = 2-13/16$, $c = 3+1/16$, $d = +1+1/8$.

A, B, C, and D represent the received

signal occurring in a given sequence or range cell for four successive pulse repetition periods. These are in chronological order, A being the oldest echo. The coefficients a through d are independent multipliers for weighting factors as previously described. Two separate solutions are calculated for each range cell, one for the in-phase component and one for the quadrature component.

Complete implementation of the canceller equation is achieved by shifting the entire digital word into a core memory 19. The memory 19 is range addressed by the range counter 28 such that each location in the memory 19 contains the three pulse history of a corresponding range cell. For each pulse transmission the oldest data in each range cell is shifted out of memory and the newest shifted in. That is, the D register 30 shifts the latest pulse into the memory 19 and subsequent registers 32, 34 and 36 shift each previous pulse with the oldest data pulse A, being shifted out of the memory 19. The four words are read simultaneously. The word representing pulse echo D is read from the A to D converter 16 while pulses C, B and A are read from the memory 19. The weighting coefficients previously discussed are applied to the data by the canceller 6. The resultant I output is resolved in less than 2.7 microseconds. Then Q is solved starting midway into the 5.4 microsecond range cell. Before the end of the 5.4 microsecond cell both I and Q have been solved and combined. The memory 19 has twice as many words as range cells to allow storage of I and Q data words. While each range cell is 5.4 microseconds, the memory 19 is capable of cycling at less than 2.5 microseconds. The circuitry performing the summing is an adder 40 fed by the arithmetic sequencer 42. The final sum from the adder 40 yields the canceller equation to an accumulator 42.

The complete arithmetic function of the canceller 6 is detailed in Fig. 4 when using only one set of weighting coefficients; in this particular case the output signals which would correspond to another set of coefficients are blanked. An arithmetic control 48 enables each of the weighted binary gates and controls the adder 40 and accumulator register 42.

The reading of the accumulator 42 takes place in 12 steps in accordance with the following table:

ACCUMULATOR READING

	Step	
	1	C
	2	A
5	3	$A - 1/8A$
	4	$A - 1/8A - 4B$
	5	$A - 1/8A - 4B + B$
	6	$A - 1/8A - 4B + B + B/8$
	7	$A - 1/8A - 4B + B + B/8 + B/16$
10	8	$A - 1/8A - 4B + B + B/8 + B/16 + 4C$
	9	$A - 1/8A - 4B + B + B/8 + B/16 + 4C - C$
	10	$A - 1/8A - 4B + B + B/8 + B/16 + 4C - C + C/16$
	11	$A - 1/8A - 4B + B + B/8 + B/16 + 4C - C + C/16 - D$
	12	$A - A/8 - 4B + B + B/8 + B/16 + 4C - C + C/16 - D - D/8$
15	Final	
	Output	$7/8 - (2 + 13/16)B + (3 + 1/16)C - (1 + 1/8)D$

The gate 60 passes the pulse or word A through without any shift whereas the gate 61 shifts the word A three places to the right to provide a binary division by 8. Likewise gate 62 passes the word B through, gate 63 shifts the word B two places to the left to provide a binary multiplication by 4, whereas gates 64 and 65 shift the word B three and four places to the right respectively to obtain division by the binary numbers 8 and 16 respectively. Word C is passed through gate 66 without any shift but is shifted two places to the left in gate 67 to provide the multiplication by 4 and four places to the right in gate 68 to provide the division by 16. Word D is passed through gate 69 without any shift and is shifted three places to the right in gate 70 to provide the division by 8.

It must be noted that when using more than one set of coefficients, the canceller 6 will comprise a sufficient number of gates to be able to provide all the coefficients. The arithmetic sequence and control unit 48 will additionally comprise a memory for storing the sets of precalculated coefficients, each set of coefficients being addressed by the rank of the transmitted pulse in the VIP cycle. The binary decoding of the coefficients will allow unit 48 to provide sequential signals to selected gates of the arithmetics sequencer 41 in order to perform the desired shifts on the digital words corresponding to the pulse amplitudes.

Further representative values of the operation of the high speed adder in the canceller 6 is a high speed synchronizer 22 which operates at a 30 megahertz clock rate. The use of high speed logic allows the solution of the complete canceller equation without adding intermediate registers and reduces processing delays.

Process delay will be 5.4 microseconds. Video sampled on a clock will be converted to a digital number in the next 1 microsecond. The second microsecond is

for propagation of the in-phase component through the arithmetic unit. Near the end of the 2.5 microsecond time, the data is clocked into the I register 80. Meanwhile Q has been converted and propagates through the arithmetic unit. At the end of 5.4 microseconds the output of both D and A converters assumes the cancelled video level. The in quadrature information Q is clocked into the Q register 82.

The digital output from the canceller 6 is converted to analog information in the two eight bit D to A converters 84 and 86. The canceller output will be digitally limited to eight bits for practical purposes. The A to D converters are of the voltage summing ladder type. The MTI video outputs are taken through a peak detector 88.

The range counter 28 counts a 185 Kiloherzt clock to define each discrete range cell. At minimum processing range the memory 18 begins to receive start pulses. Minimum range may be zero as well as any other desired range. The basic interpulse period is generated by the combined counting of the range counter 28 and the time interval counter 26. A particular pulse time-period is derived by decoding a discrete range in the range decode 27, which then initiates the time interval counter 26 at a fixed time. Another independent range-decode signals maximum range and terminates memory start signals until the next transmission.

The time interval counter 26 is set to a predetermined value and counted to initiate the transmission. The value at which the time interval counter is set is selected by the sequence control. The counter is set to the different values of the VIP cycle. A fixed PRF or VIP may be selected in the VIP sequence control 24. A frequency change trigger may be provided on a separate output if desired, once during each cycle of VIP.

The arithmetic control 48 has stored a set of four weighting coefficients (a, b, c, d) appropriate for each of the time intervals

in the VIP cycle. It operates in synchronism with the VIP sequence control to optimize the canceller for the four echoes it is processing during that specific interpulse period.

- 5 With the pulse echoes A, B, C and D each having applied thereto their respective weighting factor by the canceller 6, one is able to achieve the benefits of variable interpulse period without the penalties. In so
10 doing the width of the clutter notch is vastly improved as demonstrated by the graphical comparison of Fig. 1.

WHAT WE CLAIM IS:—

- 15 1. An MTI radar system comprising means for generating pulse radar transmissions at variable time intervals, means for extracting one or both components of the echo vectors of said pulse radar transmissions, in-phase or in quadrature with a reference signal phase-locked to the pulse radar
20 transmissions, means for sampling said component or components at regular intervals in range, means for converting each phase difference sample corresponding to a certain range cell into a digital word, means for storing at least a sequence of digital words corresponding to a same range cell, digital multiplying means for applying
25 weighting coefficients to said sequence of stored digital words and to the most recent digital word corresponding to the same range cell as the sequence, said weighting coefficients being dependent upon the time intervals between all transmitted radar
30 pulses corresponding to the digital words being weighted, means for summing said weighted sequence and most recent word to obtain a digital representation of the sum, and means for converting said digital representation to an analog video display signal.

2. An MTI radar system as claimed in claim 1 wherein the digital words representing the components of four echoes A, B, C and D are weighted by coefficients a , b , c and d respectively and the digital words resulting from the weighting operation are summed according to the relation $aA - bB + cC - dD$, a being the coefficient of oldest
45 echo, b being the coefficient of second oldest echo, c being the coefficient of third oldest echo and d being the coefficient of latest echo.

3. An MTI radar system as claimed in claim 1 or 2 wherein the storing means store a plurality of sequences of digital words cor-

responding to a plurality of range cells.

4. An MTI radar system as claimed in claim 2 or 3 wherein the weighting coefficients are:

$$a \approx 1 + \frac{3}{2} \left(\frac{\Delta T_2}{T_2} \right) + \frac{1}{2} \left(\frac{\Delta T_2}{T_2} \right)^2$$

$$d \approx 1 - \frac{3}{2} \left(\frac{\Delta T_1}{T_2} \right) + \frac{1}{2} \left(\frac{\Delta T_1}{T_2} \right)^2$$

$$b \approx 4 - d - m - k$$

$$c \approx 4 - a - m - k$$

where

$$m = 4 \left(\frac{\Delta T_1}{T_2} - \frac{\Delta T_2}{T_2} \right) - \left(\frac{\Delta T_1}{T_2} \right)^2 - \left(\frac{\Delta T_2}{T_2} \right)^2 + \left[3 - \frac{1}{2} \left(\frac{\Delta T_1}{T_2} - \frac{\Delta T_2}{T_2} \right) \left(\frac{\Delta T_1}{T_2} \right) \left(\frac{\Delta T_2}{T_2} \right) \right]$$

T_1 being the time interval between the pulse radar transmissions corresponding to echoes A and B

T_2 being the time interval between the pulse radar transmissions corresponding to echoes B and C—

T_3 being the time interval between the pulse radar transmission corresponding to echoes C and D

$$\Delta T_1 = T_2 - T_1$$

$$\Delta T_2 = T_3 - T_2$$

k being a constant which produces null in velocity response in the clutter notch region at the normalized velocity $V = \sqrt{k}/2\pi$.

5. An MTI radar system as claimed in claim 4 wherein the coefficients a , b , c and d are rounded off to the low nearest least significant digit of 1/16, the coefficients b and c being further rounded off to a lower binary value to obtain the sum $a - b + c - d$ null whereas keeping the sensitivity of the canceller constant.

6. An MTI radar system substantially as hereinbefore described with reference to and as illustrated in the accompanying drawings.

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Chartered Patent Agent.

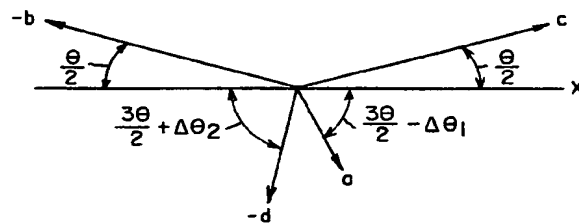
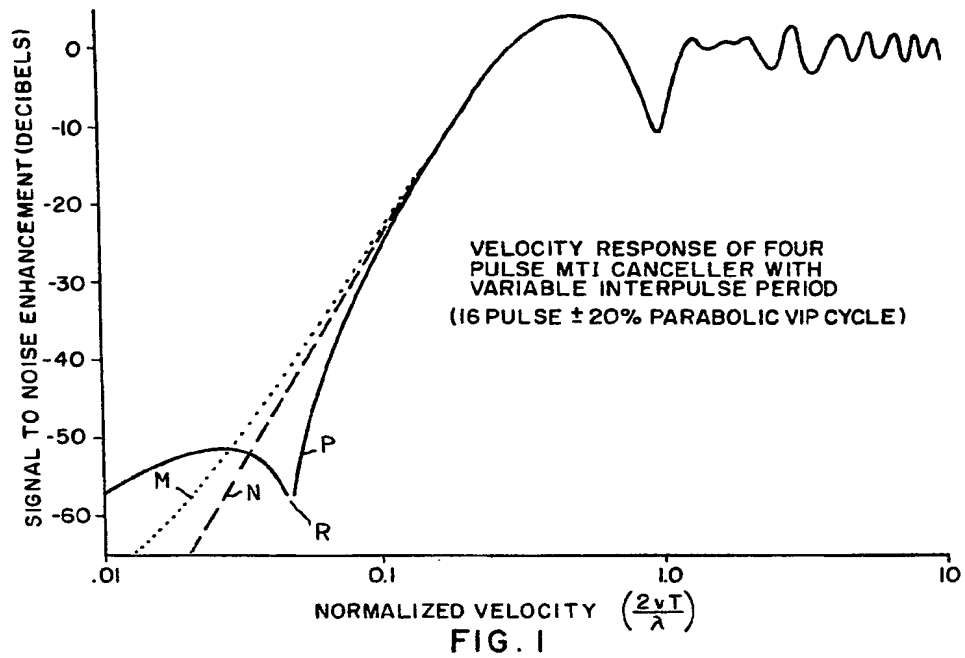
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COMPLETE SPECIFICATION

3 SHEETS

This drawing is a reproduction of
the Original on a reduced scale.
SHEET 1



**This drawing is a reproduction of
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SHEET 2

